

Divergent Triangle Integral 2: $I_3^{\{D=4-2\epsilon\}}(0, p_2^2, p_3^2; 0, 0, 0)$

Page contributed by **R.K. Ellis**

Page verified by **Lance Dixon**

$$\begin{aligned} I_3^{\{D=4-2\epsilon\}}(0, p_2^2, p_3^2, 0; 0, 0, 0) &= \frac{\mu^{2\epsilon}}{\epsilon^2} \left\{ \frac{(-p_2^2 - i\epsilon)^{-\epsilon} - (-p_3^2 - i\epsilon)^{-\epsilon}}{p_2^2 - p_3^2} \right\} \\ &= \frac{1}{p_2^2 - p_3^2} \left\{ \frac{1}{\epsilon} \left[\ln \left(\frac{\mu^2}{-p_2^2 - i\epsilon} \right) - \ln \left(\frac{\mu^2}{-p_3^2 - i\epsilon} \right) \right] + \frac{1}{2} \left[\ln^2 \left(\frac{\mu^2}{-p_2^2 - i\epsilon} \right) - \ln^2 \left(\frac{\mu^2}{-p_3^2 - i\epsilon} \right) \right] \right\} + \mathcal{O}(\epsilon) \end{aligned}$$

For $\epsilon, \varepsilon, \ln, \text{Li}_2$ see the file on **notation**.

The expression with a mass cut-off is

$$I_3^{\{D=4\}}(p_2^2, p_3^2, 0; \lambda^2, \lambda^2, \lambda^2) = \frac{1}{p_2^2 - p_3^2} \left\{ \frac{1}{2} \left[\ln^2 \left(\frac{\lambda^2}{-p_2^2 - i\epsilon} \right) - \ln^2 \left(\frac{\lambda^2}{-p_3^2 - i\epsilon} \right) \right] \right\} + \mathcal{O}(\lambda^2)$$

[Return to general page on triangles](#)

References

- [1] W. Beenakker, S. Dittmaier, M. Kramer, B. Plumper, M. Spira and P. M. Zerwas, Nucl. Phys. B **653**, 151 (2003) [[arXiv:hep-ph/0211352](#)]. [[arXiv:hep-ph/0211352](#)]